

## - CHECK THE SIZE OF THE STRUCTURES -

From the ansys results, the worst load combination exclude Element 137 in weak axis bending and Element 140(15), 203~213 in torsion are:

Element 140-0°  $F_x = 10621 \text{ lb}^{\circ}$  (Tension) or (Compression)

Element 137-0°  $F_y = 892.87 \text{ lb}$  (Shear in y-direction)

Element 140-90°  $F_z = 4790.2 \text{ lb}$  (Shear in z-direction)

Element 244-90°  $M_x = 3070.8 \text{ lb-in}$  (Torsion)

Element 137-90°  $M_y = 86115 \text{ lb-in}$  (strong axis bending)

Element 262-0°  $M_z = 3882 \text{ lb-in}$  (weak axis bending)

## - FIND THE ALLOWABLE TENSILE STRESS $F_t$ (ksi)

According to DI, AISC, ASD, Page 5-40.

The allowable stress  $F_t = 0.60 F_y$

where  $F_y = 36 \text{ ksi}$  for A36

$$F_t = 0.60 \times 36 = 21.6 \text{ ksi}$$

According to ANSI/ASME B30.20-1985, Below the Hook Lifting Devices

$$F_t = \frac{1}{3} F_y \text{ where } F_y = 36 \text{ ksi for A36}$$

$$F_t = \frac{1}{3} \times 36 = 12 \text{ ksi} \quad \text{— governs}$$

- FIND THE ALLOWABLE BENDING STRESS IN STRONG AXES  
 $F_{bx}$  (ksi)

According to Table B5.1, AISC, ASD, Page 5-36

$$\frac{bf}{2tf} = \frac{4}{2 \times 0.265} = 7.547$$

$$\frac{bf}{\sqrt{F_y}} = \frac{65}{\sqrt{36}} = 10.83 \quad \text{where } F_y = 36 \text{ ksi for A36}$$

$$\frac{bf}{2tf} < \frac{65}{\sqrt{F_y}}$$

therefore, the section is compact.

According to TABLE, AISC, ASD, Page 2-68

$$\text{for W12x16} \rightarrow L_c = 410 \text{ ft} = 49.2 \text{ m} \\ L_u = 430 \text{ ft} = 51.6 \text{ m}$$

Knowing  $L_b = 52.82 \text{ m} > L_c$

According to F4.1, AISC, ASD, Page 5-46,

The allowable bending stress in compression is determined as the larger value from EQ (F4-6), EQ (F4-7) and EQ (F4-8)

use Eq (F1-8).

$$F_{bx} = \frac{12 \times 10^3 C_b}{ld/A_f} \leq 0.60 F_y$$

where  $C_b = 1.75 + 1.05 \left( \frac{M_1}{M_2} \right) + 0.3 \left( \frac{M_1}{M_2} \right)^2$

$A_f$  = area of the compression flange, in<sup>2</sup>

$l$  = distance between cross section braced against twist or lateral displacement of the compression flange, in

$d$  = depth of the beam

Therefore,

$$C_b = 1.75 \text{ when } M_1 \ll M_2$$

$$\frac{d}{A_f} = 11.3 \text{ from page 1-28, AISC, ASD}$$

$$l = 52.82 \text{ in}$$

$$F_{bx} = \frac{12 \times 10^3 \times 1.75}{52.82 \times 11.3} = 35.18 \text{ (ksi)}$$

$$F_{bx} = 0.60 F_y \quad \text{where } F_y = 36 \text{ ksi for A36}$$

$$F_{bx} = 0.60 \times 36 = 21.6 \text{ (ksi)}$$

Since  $F_{bx} \leq 0.60 F_y$ , use  $F_{bx} = 21.6 \text{ (ksi)}$

According to ANSI/ASME B30.20-1985 Below the Hook Lifting Device

$$F_{bx} = \frac{1}{3} F_y \text{ where } F_y = 36 \text{ ksi; for A36}$$

$$F_{bx} = \frac{1}{3} \times 36 = 12 \text{ ksi; — governs}$$

- FIND THE ALLOWABLE BENDING STRESS IN WEAK AXIS  $F_{by}$ (ksi)

According to F2.2, AISC, ASD, Page 5-48

$$F_{by} = F_y \left[ 1.075 - 0.005 \left( \frac{bf}{2tf} \right) \sqrt{F_y} \right]$$

$$\text{where } F_y = 36 \text{ ksi; for A36}$$

$$\frac{bf}{2tf} = 7.5 \quad \text{— page 1-28}$$

$$F_{by} = 36 \left[ 1.075 - 0.005 \times 7.5 \times \sqrt{36} \right] = 30.6 \text{ ksi}$$

According to ANSI/ASME B30.20-1985 Below the Hook Lifting Device

$$F_{by} = \frac{1}{3} F_y \text{ where } F_y = 36 \text{ for A36}$$

$$F_{by} = \frac{1}{3} \times 36 = 12 \text{ ksi; — governs}$$

- FIND THE COMPUTED TENSILE STRESS  $f_a$  (ksi)

$$f_a = \frac{P}{A}$$

$$\text{where } P = 10621 \text{ lb}$$

$$A = 4.71 \text{ in}^2 \quad \text{— page 1-28, AISC, ASD}$$

$$f_a = \frac{10621}{4.71} = 2.2 \text{ ksi}$$

- FIND THE COMPUTED BENDING STRESS IN STRONG AXIS

$f_{bx}$  (ksi)

$$f_{bx} = \frac{M_y}{S_x} \quad \text{where } M_y = 86115 \text{ lb-in}$$

$S_x = 17.1 \text{ in}^3$  from page 1-28, AISC ASD

$$f_{bx} = \frac{86115}{17.1} = 5.04 \text{ ksi}$$

- FIND THE COMPUTED ENDING STRESS IN WEAK AXIS

$f_{by}$  (ksi)

$$f_{by} = \frac{M_z}{S_x} \quad \text{where } M_z = 3882 \text{ lb-in}$$

$S_x = 1.41 \text{ in}^3$  from page 1-28, AISC, ASD

$$f_{by} = \frac{3882}{1.41} = 2.75 \text{ ksi}$$

- FIND THE COMBINED STRESSES

According to H2, AISC, ASD, page 5-55, Eq (H2-1)

permits

$$\frac{f_a}{F_t} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0$$

where  $f_a = 2.2 \text{ ksi}$        $F_{bx} = 12 \text{ ksi}$

$F_t = 12 \text{ ksi}$        $F_{by} = 12 \text{ ksi}$

$f_{bx} = 5.04 \text{ ksi}$

$f_{by} = 2.75 \text{ ksi}$

$$\frac{2.2}{12} + \frac{5.04}{12} + \frac{2.75}{12} = 0.83 < 1.0 \quad \underline{\text{OK}}$$

$$SF = \frac{1.0}{0.83} = 1.2$$

- FIND THE ALLOWABLE COMPRESSIVE STRESS  $F_a$  ( $\text{ksi}$ )

From previous study, knowing  $\frac{bf}{2tf} < 65/\sqrt{F_y}$ .

According to AISC, ASD, Table B5.1, page 5-36, for webs in combined flexural and axial compression -

$$\frac{d}{tw} = \frac{11.99}{0.22} = 54.5$$

$$\text{for } \frac{f_u}{F_y} = \frac{2.2}{36} = 0.06 \leq 0.16 \rightarrow \frac{640}{\sqrt{F_y}} \left(1 - 3.74 \frac{f_u}{F_y}\right)$$

$$= \frac{640}{\sqrt{36}} \left(1 - 3.74 \times 0.06\right)$$

$$= 82.73$$

therefore

$$\frac{d}{tw} < \frac{640}{\sqrt{F_y}} \left(1 - 3.74 \frac{f_u}{F_y}\right) \rightarrow \text{section is compact.}$$

According to E2, AISC, ASD, page 5-42

$\frac{Kl}{r}$  where  $K$  - effective length factor  
 $l$  - length  
 $r$  - radius of gyration

when  $K=2$ ,  $l=52.82 \text{ m}$ ,  $r=0.773 \text{ in}$

$$\frac{Kl}{r} = \frac{2 \times 52.82}{0.773} = 136.66$$

According to AISC, ASD, page 5-120, the column slenderness ratio for A36 is  $C_c = 126.1$

therefore,  $\frac{Kl}{r} > C_c$

The allowable stress is permitted under E2.2

The allowable stress is permitted under the Eq (E2-2), AISC, ASD, page 5-42.

$$F_a = \frac{12\pi^2 E}{23(\frac{Kl}{r})^2} \quad \text{Eq (E2-2)}$$

where  $E = 29 \times 10^6$

$$\frac{Kl}{r} = 136.66$$

$$F_a = \frac{12 \times \pi^2 \times 29 \times 10^6}{23 \times (136.66)^2} = 7.99 \text{ ksi} - \text{governs}$$

According to ANSI/ASME, B30.20-1985 Below the Hook Lifting Device

$$F_a = \frac{1}{3} F_y \quad \text{where } F_y = 36 \text{ ksi for A36}$$

$$F_a = \frac{1}{3} \times 36 = 12 \text{ ksi}$$

### - FIND THE COMBINED STRESSES

According to H1, AISC, ASD, page 5-54, knowing

when  $\frac{f_a}{F_a} = \frac{2.2}{7.99} = 0.27 \neq 0.15$ , Eq (H1-1) &

Eq (H1-2) are permitted.

$$\frac{f_a}{F_a} + \frac{C_{mx} f_{bx}}{(1 - \frac{f_a}{F_{bx}}) F_{bx}} + \frac{C_{my} f_{by}}{(1 - \frac{f_a}{F_{by}}) F_{by}} \leq 1.0 \quad (\text{H1-1})$$

where  $f_a = 2.2 \text{ ksi}$

$$F_a = 7.99 \text{ ksi}$$

$$C_{mx} = 1$$

$$C_{my} = 1$$

$$f_{bx} = 3.04 \text{ ksi}$$

$$f_{by} = 2.75 \text{ ksi}$$

$$F_{bx} = 12 \text{ ksi}$$

$$F_{by} = 12 \text{ ksi}$$

$$F'_{ex} = \frac{12\pi^2 E}{23(k/\gamma_x)^2} = \frac{12\pi^2 \times 29 \times 10^6}{23 \times \left(\frac{2 \times 52.82}{4.67}\right)^2} = 291.8 \text{ ksi}$$

$$F'_{ey} = \frac{12\pi^2 E}{23(k/\gamma_y)^2} = 7.99 \text{ ksi}$$

Then

$$\frac{2.2}{7.99} + \frac{(1)(3.04)}{\left(1 - \frac{2.2}{291.8}\right) \times 12} + \frac{(1)(2.75)}{\left(1 - \frac{2.2}{7.99}\right) \times 12} = 1.00 \leq 1.0$$

O.K

CHECK:

$$\frac{f_a}{0.60 F_y} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0 \quad \text{EQ (H1-2)}$$

where  $f_a = 2.2 \text{ ksi}$

$$0.60 F_y = 12 \text{ ksi}$$

$$f_{bx} = 3.04 \text{ ksi}$$

$$f_{by} = 2.75 \text{ ksi}$$

$$F_{bx} = 12 \text{ ksi}$$

$$F_{by} = 12 \text{ ksi}$$

$$\frac{2.2}{12} + \frac{5.04}{12} + \frac{2.75}{12} = 0.83 \leq 1.0 \quad \underline{\text{OK}}$$

$$SF = \frac{1.0}{0.83} = 1.2$$

- FIND THE ALLOWABLE SHEAR STRESS  $F_V$  (ksi)

According to F4, AISC, ASD, Page 5-49

when  $\frac{h}{t_w} = 54.5$  for W12x16, Page 1-29, AISC. ASD

$$\frac{380}{\sqrt{F_y}} = \frac{380}{\sqrt{36}} = 63.3$$

$$\frac{b}{t_w} < \frac{380}{\sqrt{F_y}}$$

Therefore, the allowable shear stress is

$$F_V = 0.40 F_y \quad \text{where } F_y = 36 \text{ ksi for A36}$$

$$F_V = 0.40 \times 36 = 14.4 \text{ ksi}$$

According to ANSI/ASME, B30.20-1985 Below the Hook Lifting Devices

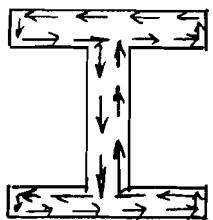
$$F_V = \frac{1}{3} F_y \quad \text{where } F_y = 36 \text{ ksi for A36}$$

$$F_V = \frac{1}{3} \times 36 = 12 \text{ ksi}$$

— governs

- FIND THE COMPUTED SHEAR STRESSES  $f_v$  (ksi)

O St Venant torsion :



According to "STRUCTURAL STEEL DESIGN"  
Chapter 7.5, Torsion , page 190

The maximum torsional shear stress in the wide-flange occurs at the center of the outer edge of the flange.

The maximum torsional shear stress can be calculated from

$$\text{flange } f_{rs} = \frac{T \times t_f}{J} \quad (\text{Eq 7.16})$$

$$\text{web } f_{rs} = \frac{T \times t_w}{J} \quad (\text{Eq 7.16})$$

where  $T$  — Torsional moment  
 $t$  — thickness of web or flange  
 $J$  — torsional constant for the entire cross section .

where  $T = 3090.8 \text{ lb-in}$

$$t_w = 0.22 \text{ in}$$

$$t_f = 0.265 \text{ in}$$

$$J = 0.10 \text{ in}^4$$

$$\text{flange: } f_{rs} = \frac{3090.8 \times 0.265}{0.10} = 8.19 \text{ ksi}$$

$$\text{web: } f_{rs} = \frac{3090.8 \times 0.22}{0.10} = 6.799 \text{ ksi}$$

o Shear stress in y-direction (flange)

$$f_{VY} = \frac{VY}{A}$$

$$\text{where } V_Y = 892.87 \text{ lb}$$

$$A = 4.71 \text{ in}^2$$

$$f_{VY} = \frac{892.87}{4.71} = 0.189 \text{ ksi}$$

o Shear stress in z-direction (web)

$$f_{VZ} = \frac{VZ}{A}$$

$$\text{where } V_Z = 4790.2 \text{ lb}$$

$$A = 4.71 \text{ in}$$

$$f_{VZ} = \frac{4790.2}{4.71} = 1.017 \text{ ksi}$$

o Combined shear stress in y-direction (flange)

$$f'_Y = f_{rs} + f_{VY}$$

$$\text{where } f_{rs} = 8.19 \text{ ksi}, \quad f_{VY} = 0.189 \text{ ksi}$$

$$f'_Y = 8.19 + 0.189 = 9.009 \text{ ksi}$$

o Combined shear stress in z-direction (web)

$$f'_Z = f_{rs} + f_{VZ}$$

where  $f_{rs} = 6.799 \text{ ksi}$ ;  $f_{vz} = 1.017 \text{ ksi}$

$$f_{vz}' = 6.799 + 1.017 = 7.816 \text{ ksi}$$

O FIND THE COMPUTED RESULTANT SHEAR STRESSES  $f_v$  (ksi)

$$\begin{aligned} f_v &= \sqrt{f_{vz}^2 + f_{vy}^2} \quad \text{where } f_{vz}' = 7.816, f_{vy}' = 9.009 \\ &= \sqrt{(7.816)^2 + (9.009)^2} \\ &= 11.92 \text{ ksi} \end{aligned}$$

O FIND THE SAFETY FACTOR ON SHEAR STRESS :

$$f_v = 11.92 \text{ ksi}$$

$$F_v = 12 \text{ ksi}$$

$$SF = \frac{12}{11.92} = 1$$

Conclusion, the cross member is adequate for the load requirement except for Element 137 in member axis bending and the torsional shear for element 141~151 and 203~213, see detail design on page 12(1)~12(13)

From the ansys results, knowing those elements suffer the maximum torsional shear stress.

$$M_x = 5569 \text{ lb-in}$$

- FIND THE COMPUTED SHEAR STRESS DUE TO TORSION.  $f_v(\text{ksi})$

According to "STRUCTURAL STEEL DESIGN" chapter 7.5 page 190, St remont torsion for wide-flange beam

$$\text{flange: } f_{vs} = \frac{T \times t_f}{J} \quad (\text{Eq 7.16})$$

$$\text{web: } f_{vs} = \frac{T \times t_w}{J} \quad (\text{Eq 7.16})$$

Where :  $T$  — Torsional moment

$t$  — thickness of web / flange

$J$  — torsional constant for the entire cross section.

When  $T = 5569 \text{ lb-in}$

$$t_f = 0.265 \text{ in}$$

$$t_w = 0.22 \text{ in}$$

$$J = 0.10 \text{ in}^4$$

$$\text{flange: } f_{vs} = \frac{5569 \times 0.265}{0.10} = 14.757 \text{ ksi}$$

$$\text{web: } f_{vs} = \frac{5569 \times 0.22}{0.10} = 12.251 \text{ ksi}$$

From previous study, knowing  $f_{vy} = 0.189 \text{ ksi}$  (flange)  
 $f_{vz} = 1.017 \text{ ksi}$  (web)

The resultant shear stress  $f_v$

$$f_v = \sqrt{(f_{vs})_{flange}^2 + (f_{vs})_{web}^2}$$

where  $(f_{vs})_{flange} = 14.757 \text{ ksi} + 0.189 \text{ ksi} = 14.946 \text{ ksi}$

$$(f_{vs})_{web} = 12.251 \text{ ksi} + 1.017 \text{ ksi} = 13.268 \text{ ksi}$$

$$f_v = \sqrt{14.946^2 + 13.268^2} = 19.98 \text{ ksi}$$

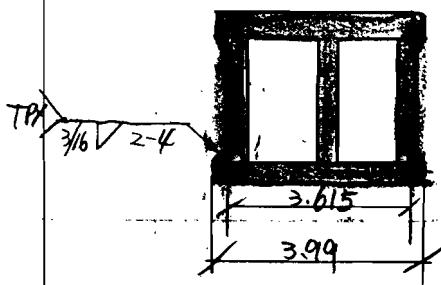
$$> F_v = 12 \text{ ksi} \\ N.G.$$

### — DESIGN THE WELD FOR TORSION PLATES

propose to weld two plates on both side of W12x16.

to take the larger shear stress.

$\leftarrow M_x$



0 FIND THE COMPUTED SHEAR STRESS  $f_s (\text{ksi})$

According to "STEEL DESIGN MANUAL"  
Chapter 7, Torsional shear stress, page  
159. For rectangular beam.

Plate:  $1/4'' \times 11\frac{1}{16}'' \times 65''$

$$f_s = \frac{T}{2bht}$$

where  $T$  — Torsional moment

$b$  — width of the tubing

$h$  — height of the tubing

$t$  — thickness of the tubing

when  $T = 5569 \text{ lb-in}$

$$b = 3.99 \text{ in}$$

$$h = 11.99 \text{ in}$$

$$t = 0.25 \text{ in}$$

$$f_s = \frac{5569}{2 \times 3.99 \times 11.99 \times 0.25} = 0.232 \text{ ksi}$$

The resultant shear stress is

$$f_r = \sqrt{(f_s + f_{ry})^2 + (f_s + f_{rz})^2}$$

$$\text{where } f_{ry} = 0.189 \text{ ksi; } f_s = 0.232 \text{ ksi;}$$

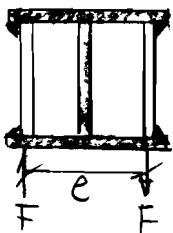
$$f_{rz} = 1.017 \text{ ksi}$$

$$f_r = \sqrt{(0.232 + 0.189)^2 + (0.232 + 1.017)^2} = 1.318 \leq 12 \text{ ksi}$$

$$SF = \frac{12}{1.318} = 9 \quad \underline{\underline{0.12}}$$

Therefore, the reinforce member is adequate to carry the shear stress due to the torsion.

## O FIND THE SHEAR STRESS ON THE WELDS.



$$\text{Known: } M_x = F \times e$$

$$\text{where } M_x = 5569 \text{ lb-in}$$

$$e = 3.615 \text{ in}$$

$$F = \frac{M_x}{e} = \frac{5569}{3.615} = 1540.5 \text{ lb}$$

For each weld:

$$F' = \frac{1}{2} F = \frac{1}{2} \times 1540.5 = 770.26 \text{ lb}$$

According to AISC, ASD. J2.2, page 5-67.

the maximum size of fillet welds is  $\frac{3}{16}$ ".

use E70XX

According to AISC, ASD. Table J2.5, page 5-70.

Knowing, the allowable stress on welds for the fillet weld on shear is

$$0.30 \times F_u \quad \text{where } F_u = 70 \text{ ksi for E70XX}$$

$$0.30 \times 70 = 21 \text{ ksi}$$

Therefore, the allowable loads in kips is

$$21 \times 0.707 \times \frac{3}{16} = 2.78 \text{ kip/in.}$$

## O FIND THE WELD LENGTH

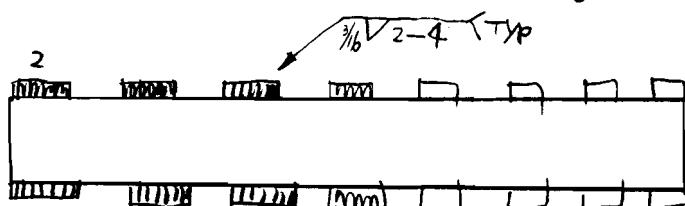
Knowing:  $F' = 770.26 = 0.770 \text{ kips}$

Welds:  $2.78 \text{ kip/in.}$

the required weld length:  $\frac{0.770}{2.78} = 0.28 \text{ in.}$

$$SF = \frac{2}{0.75} = 8$$

Use 2 in. on every element length. which equals to 4.8 in long.



## ~~MAX REINFORCEMENT PLATE FOR ELEMENT 137~~

From the ansys results, those elements suffer the maximum Bending Stress in weak axis.

	$F_x$	$F_y$	$F_z$	$M_x$	$M_y$	$M_z$
ELEMENT 137-0°	3374 lb	892 lb	3374 lb	0	60892	16072 lb-in
ELEMENT 137-45°	3374 lb	0	0	0	45698	12052 lb-in
ELEMENT 137-90°	0	892.87 lb	4772 lb	0	86115	16072 lb-in

- ① FIND THE COMPUTED AXIAL STRESS  $f_a$  (ksi)

$$f_a = \frac{P}{A}$$

where  $P = 3374 \text{ lb}$

$A = 4.71 \text{ in}^2$  from AISC, ASD, Page 1-28

$$f_a = \frac{3374}{4.71} = 0.716 \text{ ksi}$$

- ② FIND THE COMPUTED BENDING STRESS IN STRONG AXIS  $f_{bx}$  (ksi)

$$\text{ELEMENT 137-0°: } f_{bx} = \frac{M_x}{S_x} = \frac{60892}{17.1} = 3.56 \text{ ksi}$$

$$\text{ELEMENT 137-45°: } f_{bx} = \frac{M_y}{S_x} = \frac{45698}{17.1} = 2.67 \text{ ksi}$$

$$\text{ELEMENT 137-90°: } f_{bx} = \frac{M_y}{S_x} = \frac{86115}{17.1} = 5.04 \text{ ksi}$$

O FIND THE COMPUTED BENDING STRESS IN WEAK AXIS  $f_{by}$  (ksi)

$$\text{ELEMENT } 137-0^\circ \quad f_{by} = \frac{M_2}{S_y} = \frac{16072}{11.41} = 11.398 \text{ ksi}$$

$$\text{ELEMENT } 137-45^\circ \quad f_{by} = \frac{M_2}{S_y} = \frac{12054}{11.41} = 8.548 \text{ ksi}$$

$$\text{ELEMENT } 137-90^\circ \quad f_{by} = \frac{M_2}{S_y} = \frac{16072}{11.41} = 11.398 \text{ ksi}$$

O FIND THE COMBINED STRESSES

From previous study, knowing :  $F_a = 7.99 \text{ ksi}$

$$\frac{f_a}{F_a} = \frac{0.716}{7.99} = 0.089 \leq 0.15.$$

According to AISC, ASD, H1, page 5-54

Equation (H1-3) is permitted

$$\frac{f_a}{F_a} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0.$$

For Element  $137-0^\circ$ :

When,  $f_a = 0.76 \text{ ksi}$ ,  $F_a = 7.99 \text{ ksi}$ ,  $F_{bx} = 12 \text{ ksi}$ ,  $F_{by} = 12 \text{ ksi}$

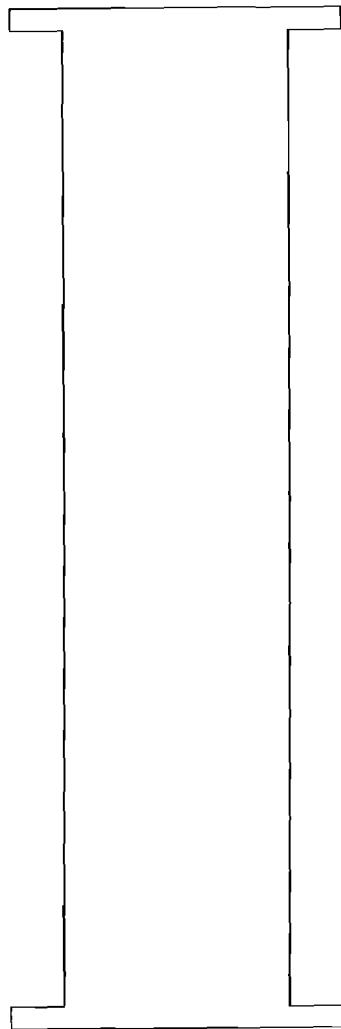
$$f_{bx} = 3.56 \text{ ksi} \quad f_{by} = 11.398 \text{ ksi}$$

$$\frac{0.76}{7.99} + \frac{3.56}{12} + \frac{11.398}{12} = 1.34 \not\leq 1.0.$$

For Element  $137-45^\circ$ :

When :  $f_a = 0.76 \text{ ksi}$ ,  $F_a = 7.99 \text{ ksi}$ ;  $F_{bx} = 12 \text{ ksi}$

$$F_{by} = 12 \text{ ksi}, \quad f_{bx} = 2.67 \text{ ksi}; \quad f_{by} = 8.548 \text{ ksi}$$



Area=3.32859e+01  
Xcg=-1.30596e+01  
Ycg=-3.16964e+00  
~~Iyprin=4.14098e+02~~  
~~Iycg=2.19141e+01~~  
Ixycg=2.86678e-01  
Ixor=7.48509e+02  
Iyor=5.69896e+03  
Ixyor=1.37814e+03  
Kxcg=3.52713e+00  
Kycg=8.11394e-01  
Kxor=4.74207e+00  
Kyor=1.30848e+01  
Ixprin=2.19139e+01  
Iyprin=4.14098e+02  
Ipolar=4.36012e+02

$$\frac{0.76}{7.99} + \frac{2.67}{12} + \frac{8.548}{12} = 1.029 \neq 1.0$$

For Element B7-90°

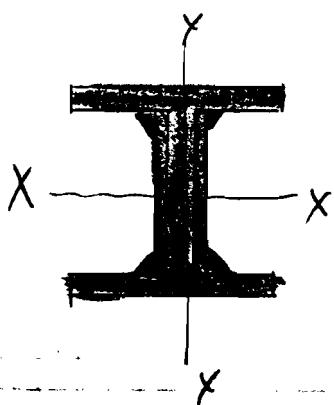
When,  $f_a = 0$ ,  $F_a = 7.99 \text{ ksi}$ ,  $F_{bx} = 12 \text{ ksi}$

$F_{by} = 12 \text{ ksi}$     $f_{bx} = 5.04 \text{ ksi}$     $f_{by} = 11.398 \text{ ksi}$

$$\frac{0}{7.99} + \frac{5.04}{12} + \frac{11.398}{12} = 1.37 \neq 1.0$$

#### - DESIGN THE REINFORCEMENT PLATES ON WEB

Propose to weld two plates on both side of the web  
to take the large bi-axial bending stress.



From the ideas results. knowing

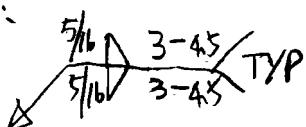
$$I_x = 414 \text{ in}^4$$

$$I_y = 21.9 \text{ in}^4$$

then,

Plate:  $1\frac{1}{4}'' \times 11\frac{7}{16}'' \times 30''$  long

weld:



$$S_x = \frac{I_x}{y} = \frac{414}{(\frac{11.99}{2})} = 69.86 \text{ in}^3$$

$$S_y = \frac{I_y}{x} = \frac{21.9}{(\frac{3.99}{2})} = 10.97 \text{ in}^3$$

O FIND THE COMPUTED BENDING STRESS IN STRONG AXIS  $f_{bx}$  (ksi)

$$\text{ELEMENT 137-0}^\circ \quad f_{bx} = \frac{M_x}{S_x} = \frac{60892}{69.06} = 0.882 \text{ ksi}$$

$$\text{ELEMENT 137-45}^\circ \quad f_{bx} = \frac{M_x}{S_x} = \frac{45698}{69.06} = 0.662 \text{ ksi}$$

$$\text{ELEMENT 137-90}^\circ \quad f_{bx} = \frac{M_x}{S_x} = \frac{86115}{69.06} = 1.247 \text{ ksi}$$

O FIND THE COMPUTED BENDING STRESS IN WEAK AXIS  $f_{by}$  (ksi)

$$\text{ELEMENT 137-0}^\circ \quad f_{by} = \frac{M_z}{S_y} = \frac{16072}{10.97} = 1.465 \text{ ksi}$$

$$\text{ELEMENT 137-45}^\circ \quad f_{by} = \frac{M_z}{S_y} = \frac{12054}{10.97} = 1.099 \text{ ksi}$$

$$\text{ELEMENT 137-90}^\circ \quad f_{by} = \frac{M_z}{S_y} = \frac{16072}{10.97} = 1.465 \text{ ksi}$$

O FIND THE COMPUTED COMPRESSIVE STRESS  $f_a$  (ksi)

$$f_a = \frac{P}{A} \quad \text{where } P = 3374 \text{ lb}$$

$A = 33.3 \text{ in}^2$  from ideal results

$$f_a = \frac{3374}{33.3} = 0.104 \text{ ksi}$$

O FIND THE ALLOWABLE COMPRESSIVE STRESS  $F_a$  (ksi)

According to AISC, ASD, Table B5.1, page 5-36,

knowing, for welded beam in flexure.

$$\frac{b}{t} = \frac{3.99}{2(0.22 + 1.25 + 1.25)} = 0.73$$

$$\frac{65}{F_f} = \frac{65}{\sqrt{36}} = 10.83$$

$$\frac{b}{t} < \frac{65}{\sqrt{F_y}}$$

for web in combined flexural and axial compression

$$\frac{d}{tw} = \frac{11.99}{(0.22 + 1.25 + 1.25)} = 4.4$$

when  $f_a = 0.101 \text{ ksi}$ ;  $F_y = 36 \text{ ksi}$  for A36

$$\frac{f_a}{F_y} = \frac{0.101}{36} = 0.003 \leq 0.16$$

then

$$\frac{640}{\sqrt{F_y}} \left( 1 - 3.74 \frac{f_a}{F_y} \right) = \frac{640}{\sqrt{36}} \left( 1 - 3.74 \times 0.003 \right) \\ = 105.5$$

therefore,

$$\frac{d}{tw} < \frac{640}{\sqrt{F_y}} \left( 1 - 3.74 \frac{f_a}{F_y} \right)$$

This section meets the provisions of the AISC, ASD for compact.

According to E2, AISC, ASD, page 5-42

$\frac{Kl}{r}$  where  $K$  = effective length factor

$l$  = length

$r$  = radius of gyration

When  $k=2$

$$l = 52.82 \text{ m}$$

$$r = \sqrt{\frac{I}{A}} \text{ where } I = 21.9 \text{ in}^4 \quad A = 33.3 \text{ in}^2$$

$$r = \sqrt{\frac{21.9}{33.3}} = 0.81 \text{ in}$$

$$\frac{kl}{r} = \frac{2 \times 52.82}{0.81} = 130.26$$

From previous study, knowing  $C_c = 126.1$

$$\text{therefore } \frac{kl}{r} < C_c$$

The allowable stress is permitted in Eq (E2-2)

$$F_a = \frac{12\pi^2 E}{23(kl/r)^2}$$

$$\text{where } E = 29 \times 10^6$$

$$\frac{kl}{r} = 130.26$$

$$F_a = \frac{(12 \times \pi^2 \times 29 \times 10^6)}{23 \times (130.26)^2} = 8.8 \text{ ksi - governs}$$

According to ANSI/ASME B30.20-1985, Below the Hook Lifting Device, knowing:

$$F_a = \frac{1}{3} F_y \text{ where } F_y = 36 \text{ ksi for A36}$$

$$F_a = \frac{1}{3} \times 36 = 12 \text{ ksi}$$

- FIND THE COMBINED STRESSES.

According to H4, AISC, ASD, page 5-54, providing

When  $\frac{f_a}{F_a} = \frac{0.101}{8.8} = 8.8 \times 10^{-7} < 0.15$ , EQ (H4-3)  
is permitted

$$\frac{f_a}{F_a} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0 .$$

For Element 137-0°

When  $f_a = 0.101 \text{ ksi}$ ;  $F_a = 8.8 \text{ ksi}$ ;  $f_{bx} = 0.882 \text{ ksi}$ ;  
 $F_{bx} = 12 \text{ ksi}$ ;  $f_{by} = 1.465 \text{ ksi}$ ;  $F_{by} = 12 \text{ ksi}$

$$\frac{0.101}{8.8} + \frac{0.882}{12} + \frac{1.465}{12} = 0.21 < 1.0 \quad \underline{\text{OK}}$$

$$SF = \frac{1.0}{0.21} = 4.8$$

For Element 137-45°

When  $f_a = 0.101 \text{ ksi}$ ;  $F_a = 8.8 \text{ ksi}$ ;  $f_{bx} = 0.662 \text{ ksi}$ ;  
 $F_{bx} = 12 \text{ ksi}$ ;  $f_{by} = 1.099 \text{ ksi}$ ;  $F_{by} = 12 \text{ ksi}$

$$\frac{0.101}{8.8} + \frac{0.662}{12} + \frac{1.099}{12} = 0.16 < 1.0 \quad \underline{\text{OK}}$$

$$SF = 6.3$$

For Element 137-90°

When  $f_a = 0$ ;  $F_a = 8.8 \text{ ksi}$ ;  $f_{bx} = 1.247 \text{ ksi}$ ;  
 $F_{bx} = 12 \text{ ksi}$ ;  $f_{by} = 1.465 \text{ ksi}$ ;  $F_{by} = 12 \text{ ksi}$

$$\frac{0}{8.8} + \frac{1.247}{12} + \frac{1.465}{12} = 0.23 < 1.0 \quad \text{OK}$$

$$SF = \frac{1.0}{0.23} = 4.3$$

Therefore, the reinforced member is adequate for taking the larger bi-axial bending stress.

### - DESIGN THE WELDS FOR BENDING MOMENT ONLY

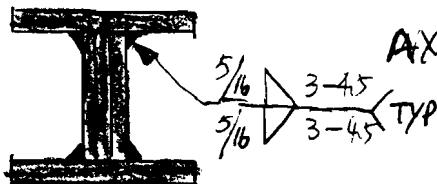
From the ansys results, knowing the bending moments at the strong axis and weak axis are:

Elements 137-90°

$M_y$   
86115 lb-in

$M_z$   
16072 lb-in

O FIND THE BENDING STRESS IN STRONG AXIS AT POINT OF WELDS



$$f_{bx} = \frac{M_y}{I_x}$$

where  $M_y = 86115 \text{ lb-in}$

$$Y = \frac{11.99}{2} - 0.265 = 5.73 \text{ in}$$

$$I_x = 414 \text{ in}^4$$

$$f_{bx} = \frac{86115 \times 5.73}{414} = 1.192 \text{ ksi}$$

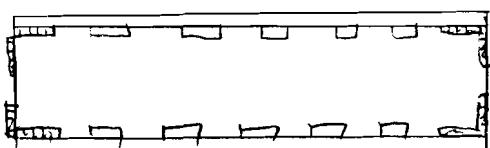
O FIND THE BENDING STRESS IN WEAK AXIS AT POINT OF WELDS

$$f_{by} = \frac{M_z X}{I_y}$$

where  $M_z = 16072 \text{ lb-in}$

$$X = \frac{1}{2} \times (0.22 + 2 \times 1.25) = 1.36 \text{ in}$$

$$I_y = 27.9 \text{ in}^4$$



$$f_{by} = \frac{16072 \times 1.36}{21.9} = 0.998 \text{ ksi}$$

- O FIND THE COMBINED BENDING STRESS AT POINT OF WELD

$$f_{\text{combined}} = \frac{1}{2} \times 1.192 + \frac{1}{2} \times 0.998 = 1.095 \text{ ksi}$$

- O FIND THE ALLOWABLE STRESS ON THE WELDS

According to AISC, ASD, Table J2.5, page 3-70, knowing for fillet welds under tension or compression parallel to axis of weld, the allowable stress is the same as the base metal. According to ANSI-ASME, B30.20-1993, Below the Hook Lifting Device, knowing, the allowable is  $\frac{1}{3} F_y$  where  $F_y = 36 \text{ ksi}$  for A36

$$\text{Allow.} = \frac{1}{3} \times 36 = 12 \text{ ksi}$$

- O FIND THE ALLOWABLE LOAD ON THE WELDS.

According to AISC, ASD, J2.2a, Page 5-67. knowing the size of fillet weld is  $\frac{5}{16}$ ", using E70XX weld then,  $0.707 \times \frac{5}{16} \times 12 = 2.65 \text{ kips/in}$

- O FIND THE REQUIRED LENGTH OF THE WELD.

$$\frac{2.65}{1.095} = 2.4 \text{ in per element (4.5" long)}$$

$$\text{use } 3" \rightarrow SF = \frac{3}{2.4} = 1.3$$

In conclusion, the cross member design is accurate to carry the load requirement.

~~TECHNICAL DRAWING~~ ~~4 x 5/8~~

From the ANSYS results, the worst load combination will be:

Element 116-0°  $F_x = 2646.9 \text{ lb}$  (compression)

Element 62-0°  $F_y = 3429.5 \text{ lb}$  (shear in y-direction)

Element 124-90°  $F_z = 2457 \text{ lb}$  (shear in z-direction)

Element 116-90°  $M_x = 18949 \text{ lb-in}$  (Torsion)

Element 1-45°  $M_y = 89099 \text{ lb-in}$  (Strong axis bending)

Element 63-0°  $M_z = 52055 \text{ lb-in}$  (Weak axis bending)

- FIND THE COMPUTED AXIAL STRESS  $f_a$  (ksi)

$$f_a = \frac{P}{A}$$

where  $P = 2646.9 \text{ lb}$

$A = 9.36 \text{ in}^2$  from page 1-98, AISI, ASD

$$f_a = \frac{2646.9}{9.36} = 0.283 \text{ ksi}$$

- FIND THE ALLOWABLE COMPRESSIVE STRESS  $F_a$  (ksi)

According to Table B3.1, AISI, ASD, page 5-36,

Flanges of rectangular box subject to bending

or compression

$$\frac{b}{t}$$

According to AISC, ASD, page 5-120,  $C_c$  is the column slenderness ratio, for A500 grade B tubing ( $F_y = 46 \text{ ksi}$ )

$$C_c = 111.6$$

Therefore  $\frac{Kl}{r} < C_c$

The allowable stress is permitted under Eq (Eq.1)

$$F_a = \frac{\left[1 - \frac{(Kl/r)^2}{2C_c^2}\right] F_y}{\frac{5}{3} + \frac{3(Kl/r)}{8C_c} - \frac{(Kl/r)^3}{8C_c^3}} \quad \text{--- (Eq.1)}$$

AISC, ASD, Page 5-42.  
Eq.1

where

$$C_c = 111.6$$

$$\frac{Kl}{r} = 70.43$$

$$F_a = \frac{\left[1 - \frac{70.43^2}{2 \times 111.6^2}\right] \times 46}{\frac{5}{3} + \frac{3 \times 70.43}{8 \times 111.6} - \frac{70.43^3}{8 \times 111.6^3}} = 19.68 \text{ ksi}$$

According to ANSI/ASME, B30.20-1985 Below the Hook Lifting Device

$$F_a = \frac{1}{3} F_y \text{ where } F_y = 46 \text{ ksi for A500 grade B tubing}$$

$$F_a = \frac{1}{3} \times 46 = 15.33 \text{ ksi} \quad \text{--- 30 rems}$$

- FIND THE ALLOWABLE BENDING STRESS IN STRONG AXIS  
 $F_{bx}$  (ksi)

According to F3, AISC, ASD, Page 5-48, To be classified as a compact section, in addition to the requirements in section B 5, a depth not greater than 6 times the width, a flange thickness not greater than 2 times the web thickness and the laterally unsupported length  $L_b$  less than or equal to  $EQ(F3-2)$ .

$$L_c = (1950 + 1200 \frac{M_1}{M_2}) \frac{b}{F_y}$$

When  $d = 12$  in

$$6 \text{ times the width} = 6 \times 4 = 24 \text{ in}$$

$d \neq 6$  times the width

OK

When  $t = 0.3125$  in

$$2 \text{ times the thickness} = 2 \times 0.3125 = 0.625 \text{ in}$$

$t \neq 2$  times the thickness

OK

When  $L_b = 59.51$  in

$$L_c = (1950 + 1200 \frac{M_1}{M_2}) \frac{b}{F_y}$$

where  $b = 1.0625$  in

$F_y = 46$  ksi; for A500 Grade B tubing.

Assume  $M_1 \ll M_2$

Then

$$L_c = (1950) \times \frac{1.0625}{46} = 45.04 \text{ in}$$

$$L_b > L_c$$

Therefore, this member is the non compact section.

According to F3.2, AISC, ASD, page 5-49  
the allowable stress is

$$F_{bx} = 0.60 F_y \quad \text{where } F_y = 46 \text{ ksi for A 500 grade B tubing}$$

$$F_{bx} = 0.60 \times 46 = 27.6 \text{ ksi}$$

According to ANSI/ASME B30.20-1985, Below the Hook Lifting device

$$F_{bx} = \frac{1}{3} F_y \quad \text{where } F_y = 46 \text{ ksi for A 500 grade B tubing}$$

$$F_{bx} = \frac{1}{3} \times 46 = 15.33 \text{ ksi} - \text{governed}$$

- FIND THE ALLOWABLE BENDING STRESS IN WEAK AXIS  $F_{by}$  (ksi)

According to F3.2, AISC, ASD, page 5-49

$$F_{by} = 0.60 F_y \quad \text{where } F_y = 46 \text{ ksi; for A36 grade B tubing}$$

$$F_{by} = 0.60 \times 46 = 27.6 \text{ ksi}$$

According to ANSI/ASME, B30.20-1985 Below the Hook  
Lifting Devices

$$F_{by} = \frac{1}{3} F_y \quad \text{where } F_y = 46 \text{ ksi; for A36 grade B tubing}$$

$$F_{by} = \frac{1}{3} \times 46 = 15.33 \text{ ksi}$$

— given

- FIND THE COMPUTED BENDING STRESS IN STRONG AXIS  $f_{bx}$  (ksi)

$$f_{bx} = \frac{M}{S_x}$$

where  $M = 89099 \text{ lb-in}$

$S_x = 25.5 \text{ in}^3$  from page 1-98, AISC, ASD.

$$f_{bx} = \frac{89099}{25.5} = 3.49 \text{ ksi}$$

- FIND THE COMPUTED BENDING STRESS IN WEAK AXIS  $f_{by}$  (ksi)

$$f_{by} = \frac{M}{S_y}$$

where  $M = 52055 \text{ lb-in}$

$S_y = 13.3 \text{ in}^3$  from page 1-98, AISC, ASD

$$f_{by} = \frac{52055}{13.3} = 3.913 \text{ ksi}$$

- FIND THE COMBINED STRESSES

According to H4, AISC, ASD, page 5-54, knowing  
when

$$\frac{f_a}{F_a} = \frac{0.283}{15.33} = 0.018 \leq 0.15$$

EQ (H1-3) is permitted.

Therefore,

$$\frac{f_a}{F_a} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}} \leq 1.0$$

where  $f_a = 0.283 \text{ ksi}$ ,

$$F_a = 15.33 \text{ ksi}$$

$$f_{bx} = 3.49 \text{ ksi}$$

$$F_{bx} = 15.33 \text{ ksi}$$

$$f_{by} = 3.913 \text{ ksi}$$

$$F_{by} = 15.33 \text{ ksi}$$

$$\frac{0.283}{15.33} + \frac{3.49}{15.33} + \frac{3.913}{15.33} = 0.50 \leq 1.0$$

OK

$$SF = \frac{1.0}{0.50} = 2$$

- FIND THE ALLOWABLE SHEAR STRESS  $F_v$  (ksi)

According to T4. AISC, ASD, page 5-49, when

$$\frac{h}{t_w} = \frac{12}{2 \times 0.3125} = 19.2$$

$$\frac{380}{\sqrt{F_y}} = \frac{380}{\sqrt{46}} = 56$$

$\frac{h}{t_w} < \frac{380}{\sqrt{F_y}}$ . therefore, the allowable shear stress is

$$F_v = 0.40 F_y \quad \text{where } F_y = 46 \text{ ksi for A360 grade B tubing}$$

$$F_v = 0.40 \times 46 = 18.4 \text{ ksi}$$

According to ANSI/ASME, B30.20-1985, Below the Hook Lifting Devices

$$F_v = \frac{1}{3} F_y \quad \text{where } F_y = 46 \text{ ksi for A360 grade B tubing}$$

$$F_v = \frac{1}{3} \times 46 = 15.33 \text{ ksi}$$

— 300 reens

According to "STEEL DESIGN MANUAL"

Chapter 7, Torsion, Page 159

The shear stresses in a closed rectangular section subject to torsion are parallel to the sides of the sections. The shear flow has a uniform value along both sides, and when moments at the corners are summed, the shear stresses along side is

$$f_s = \frac{T}{2bt}$$

where  $T$  — Torsional moment

$b$  — width of the tubing

$b$  — height of the tubing

$t$  — thickness of the tubing

$$= 18949 \text{ lb-in}$$

$$= 4 \text{ in}$$

$$= 12 \text{ in}$$

$$= 0.3125 \text{ in}$$

$k_s$

$f_{Vx}$

Page 1-98, AISC, ASD

$i$

$\bar{v}_z$

Page 1-98, AISC, ASD

'-direction

0.997  $k_s$

- Combined shear stresses in  $z$ -direction

$$f'_{rz} = f_s + f'_{vz}$$

where  $f_s = 0.631 \text{ ksi}$

$$f'_{vz} = 0.262 \text{ ksi}$$

$$f'_{rz} = 0.631 + 0.262 = 0.893 \text{ ksi}$$

- The computed resultant shear stresses  $f_r$  ksi:

$$f_r = \sqrt{f'_{ry}^2 + f'_{rz}^2}$$

where  $f'_{ry} = 0.997 \text{ ksi}$

$$f'_{rz} = 0.893 \text{ ksi}$$

$$f_r = \sqrt{0.997^2 + 0.893^2} = 1.338 \text{ ksi}$$

- FIND THE SAFETY FACTOR ON SHEAR STRESS :

$$f_r = 1.338 \text{ ksi}$$

$$F_r = 15.33 \text{ ksi}$$

$$SF = \frac{15.33}{1.338} = 11.5$$

In conclusion, the frame member is adequate to carry the load requirement.